Benefits of Restricting Trading Opportunities in a Dynamic Lemons Market

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• Toxic assets and a role for TARP like interventions.

• Static:

• Akerlof (1970), Samuelson (1984)

• Dynamic: Markets for lemons and signaling

- Noldeke and vanDamme 1990 and Swinkels 1999
- Jansen and Roy (2002), Daley and Green (2012).
- Matching: Guerrieri and Shimer (2011-13). Chang (2012)

• Government Interventions:

- Philipon and Skreta (2012)
- Tirole (2012)

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 - "Infrequent trading": $\Omega_I = \{0, T\}$
 - Continuous trading: $\Omega_{\mathcal{C}} = [0, T]$
- If trade happens at time t at a price p_t then the payoffs are :

Seller :
$$(1 - e^{-rt}) c + e^{-rt} p_t$$

Buyer: $e^{-rt} (v (c) - p_t)$

- A competitive equilibrium of this market is a pair of functions $\{p_t, k_t\}$ for $t \in \Omega$. These functions must satisfy:
 - Zero profit condition: $p_t = E[v(c) | c \in [k_{t-}, k_t]]$

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 - Zero profit condition: $p_t = E[v(c) | c \in [k_{t-}, k_t]]$
 - Seller's optimality
 - Market Clearing: in any period the market is open $p_t \ge v(k_{t-})$.

Proposition (Infrequent/Restricted Trading)

For $\Omega = \{0, T\}$ there exists a competivie equilibrium $\{p_0, k_0\}$. Equilibria are a solution to:

$$p_0 = E[v(c) | c \in [0, k_0]]$$
 (1)

$$p_0 = \left(1 - e^{-rT}\right) k_0 + e^{-rT} v(k_0)$$
(2)

If $\frac{f(c)}{F(c)}(v(c)-c) - \frac{e^{-rT}}{1-e^{-rT}}v'(c)$ is strictly decreasing then the equilibrium is unique.

- Buyers break-even condition.
- Seller's optimality condition.

Equilibrium with Continuous Trading

With continuous trading, $\Omega_{\mathcal{C}} = [0, T]$.

No atoms (follows from p_t ≥ v (k_t-)) & the zero profit condition imply:

$$p_t = v(k_t).$$

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• These conditions yield a differential equation for the cutoff type

$$r\left(v\left(k_{t}\right)-k_{t}\right)=v'\left(k_{t}\right)\dot{k}_{t}$$

with the boundary condition $k_0 = 0$.

Proposition (Continuous trading)

For $\Omega = [0, T]$ the competitive equilibrium is the unique solution to:

$$p_t = v(k_t)$$

$$k_0 = 0$$

$$r(v(k_t) - k_t) = v'(k_t)\dot{k}_t$$

Let c be distributed uniformly over [0, 1] and $v(c) = \frac{1+c}{2}$.



The solution for $\Omega_I = \{0, T\}$ is:

$$k_0 = rac{2 - 2e^{-rT}}{3 - 2e^{-rT}}$$
 $p_0 = rac{4 - 3e^{-rT}}{6 - 4e^{-rT}}$

The solution for $\Omega_{\mathcal{C}} = [0, T]$ is:

$$k_t = 1 - e^{-rt}$$

 $p_t = \frac{1 + (1 - e^{-rt})}{2}$

Example: Dynamics of Trade



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Which is more efficient?

We graph the ratio $\frac{S_{FB}-S_c}{S_{FB}-S_l}$ for our example:



When the private information is long lived the efficiency loss with continuous trading is three times higher than with infrequent

Fuchs-Skrzypacz (Berkeley Stanford)

Restricting Trade

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- In Spence's signaling model the first best outcome is achieved by closing down the school.
- Here restricting trading opportunities comes at a cost because some types will never trade as a result.
- Restricting trading opportunities may actually be welfare reducing.

There exist v(c) and F(c) such that for T large enough the continuous trading market generates more gains from trade than the infrequent trading market

• Proof by Example: $v(c) = \frac{1+c}{2}$ but F(c) with a lot of mass for $c \in [0, \varepsilon]$ little mass for $c \in [\varepsilon, k_0]$ and a lot of mass for $c \in (k_0, 1)$.

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- Mass above *k*₀ : unrealized surplus with infrequent trading reached with continuous trading after some delay.

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- **()** Closing the market **briefly** after **innitial** trade always good. **Pareto**
- **2** Infrequent trading optimal under certain (fairly general) conditions.
- Solution Closing the market briefly at other times is a wash.

Suppose we start from continuous trading and we introduce a short pause of length Δ after the initial trade.

$$\Omega^{EC} = \{\mathsf{0}, [\Delta, T]\}$$

Theorem

For every r, T, F (c), and v (c), there exists $\Delta > 0$ such that the early closure market design $\Omega^{EC} = \{0\} \cup [\Delta, T]$ yields higher gains from trade than the continuous trading design $\Omega_C = [0, T]$.

Closing the Market Briefly after Initial Trade

Proof.

To establish that early closure increases efficiency of trade we show an even stronger result: that for small Δ with Ω^{EC} there is more trade at t = 0 than with Ω_C by $t = \Delta$. Let k_{Δ}^{EC} be the highest type that trades at t = 0 when the design is Ω^{EC} . Let k_{Δ}^{C} the equilibrium cutoff at time Δ in design Ω_C . Then the stronger claim is that for small Δ , $k_{\Delta}^{C} < k_{\Delta}^{EC}$. Since $\lim_{\Delta \to 0} k_{\Delta}^{EC} = \lim_{\Delta \to 0} k_{\Delta}^{C} = 0$. So it is sufficient for us to rank:

$$\lim_{\Delta \to 0} \frac{\partial k_{\Delta}^{EC}}{\partial \Delta} \text{ vs. } \lim_{\Delta \to 0} \frac{\partial k_{\Delta}^{C}}{\partial \Delta}$$

Indeed we can show:

$$\lim_{\Delta \to 0} \frac{\partial k_{\Delta}^{EC}}{\partial \Delta} = 2 * \lim_{\Delta \to 0} \frac{\partial k_{\Delta}^{C}}{\partial \Delta}$$

Definition

We say that the environment is *regular* if $\frac{f(c)}{F(c)} \frac{v(c)-c}{1-\delta+\delta v'(c)}$ and $\frac{f(c)}{F(c)} (v(c)-c)$ are decreasing.

- A sufficient condition is that $v''(c) \ge 0$ and $\frac{f(c)}{F(c)}(v(c)-c)$ is decreasing.
- Similar to the standard condition in optimal auction theory/pricing theory that the virtual valuation/marginal revenue curve be monotone.
- The static problem of a monopsonist buyer choosing a cutoff (or a probability to trade, F(c)), by making a take-it-or-leave-it offer equal to $P(c) = (1 \delta) c + \delta v(c)$, there $\frac{f(c)}{F(c)} \frac{v(c) c}{1 \delta + \delta v'(c)}$ decreasing guarantees that the marginal profit crosses zero exactly once.

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Theorem

If the environment is regular then infrequent trading, $\Omega_I = \{0, T\}$, generates higher expected gains from trade than any other market design.

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- We expand the set of possible market designs to **allow for any trading mechanism** that is incentive compatible, does not require the buyers to lose money **on average**.
- For every market design, the equilibrium outcome can be replicated by such a mechanism (but not necessarily vice versa).
- We then show that under the regularity condition infrequent trading replicates the outcome of the best mechanism and hence any other market design generates lower expected gains from trade.

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- For $T = \infty$ time of trade and probability of trade are essentially equivalent relating to the static result of Samuelson (1984).

One way to implement $\Omega_I = \{0, T\}$ in practice may be via an extreme anonymity of the market. In our model we have assumed that the initial seller of the asset can be told apart in the market from buyers who later become secondary sellers. However, if the trades are completely anonymous, even if $\Omega \neq \{0, T\}$, the equilibrium outcome would coincide with the outcome for Ω_I . The reason is that the price can never go up since otherwise the early buyers of the low-quality assets would resell them at the later markets. Suppose we start from continuous trading and we introduce a short pause of length Δ before T.

$$ilde{\Omega} = \{ [\mathsf{0}, \, \mathcal{T} - \Delta, \,] \, , \, \mathcal{T} \}$$

Closing the Market Briefly before Information Arrives. Efficiency loss from Endogenous Closure:

If the market is closed from T − Δ to T, there will be an atom of types [k_{t*}, k_{T−Δ}] trading at T − Δ.

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S As a result there need to be "quiet period" before T − Δ : there will be some time interval [t*, T − Δ) where despite the market being open, there will be no types that would trade.

$$\left(1-e^{-r(T-\Delta-t^*)}\right)k_{t^*}+e^{-r(T-\Delta-t^*)}p_{T-\Delta}=v\left(k_{t^*}\right)$$

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Before t* the equilibrium outcome remains unchanged

Closing the Market Briefly before Information Arrives Endogenous Closure:



$$T = 10$$
 $\Delta = 1$ $r = 0.1$ $v(c) = \frac{c+1}{2}$ $F(c) = c$

 We assumed v (0) > 0. If instead v (0) = 0 then we could have cases in which the is no Ω for which any amount of trade can take place. For example if F (c) = c and v (c) = γc for γ ∈ (1, 2). This model arrises for example if the seller has a higher discount rate than the buyers. Banks in 2009 vs W.Buffet

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- If the goverment steps in and removes the most "toxic" assets from the market.
 - Buy anything banks are willing to sell for $\gamma \epsilon$.
 - We are left with $c \in [\varepsilon, 1]$ and now we can let the market take over.
- In general, the surplus/gain from trades far outweighs the government investmentment of $\gamma \varepsilon^2$.
- Even banks that do not sell to the government benefit from this type of intervention.

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- When thinking about organizing markets an additional consideration is what information is revealed. Fuchs, **Öry** and Skrzypacz (2013)