

# Module 13: Information Disclosure

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## Unraveling and the Full Disclosure Theorem

- Informed seller and 2 risk-neutral uninformed buyers (Bertrand competition).
- Quality  $\theta_i \in \{\theta_1, \dots, \theta_N\}$  of product is known privately by the seller
  - Buyers hold probability distribution over  $\theta_i$  and  $\mathbb{E}[\theta_i] = \bar{\theta}$ .
- Seller can make verifiable costless disclosure about product quality.
  - Seller cannot make manifestly false claim (as opposed to cheap talk).
  - If quality is  $\theta_i$  then can report  $r_i = \{\theta_i, \dots, \theta_N\}$  (“quality of my product is at least  $\theta_i$ ”) or not disclose  $r_i = \emptyset$ .
- Buyer observes disclosure and chooses to offer price  $p$ .
- Final payoffs are
  - Buyer:  $U_S = p$
  - Seller:  $U_B = \theta - p$
- Equilibrium price (due to Bertrand competition):  $p(r_i) = \mathbb{E}[\theta_i | r_i]$

## Analysis

- Consider seller of the highest quality  $\theta_N$ .
  - Strict incentive to disclose quality since  $\mathbb{E}[\theta_i | r_i = \emptyset] < \theta_N$

- If the highest-quality seller discloses, then if a seller does not disclose, his quality can be at most  $\theta_{N-1}$ .
- Now, consider seller of second-highest quality  $\theta_{N-1}$ .
  - Strict incentive to disclose since  $\mathbb{E}[\theta_i | r_i = \emptyset] < \theta_{N-1}$ .
  - Therefore, if a seller does not disclose, his quality can be at most  $\theta_{N-1}$ .
- ... and so on!

### Full Disclosure

- To complete induction argument, suppose that seller of quality  $\theta_i > \theta_1$  does not disclose.
- Consider choice of the seller of quality  $\theta_j \geq \theta_i$ 
  - Disclose quality  $\theta_j$ : receive  $p = \theta_j$
  - Do not disclose: get pooled with  $\theta_i$  and  $\theta_1$  (for whom disclosing is weakly dominated) and receive lower price.
- *Result:* Unraveling and full disclosure!
  - Why do we need mandatory disclosure laws?
- ... but it relies heavily on rather strong assumptions!
  - Sellers must always be perfectly informed about their quality.
  - Absence of disclosure costs.

### Imperfectly Informed Sellers

- Simplified setting where  $\theta_i \in \{\theta_B, \theta_G\}$  and  $\theta_B < \theta_G$  with  $\Pr(\theta_i = \theta_G) = \beta$ .
  - Seller can disclose type or not disclose.
- Sellers are imperfectly informed:
  - with probability  $\gamma < 1$ , seller is informed ; and
  - with probability  $1 - \gamma$ , seller is uninformed (like buyer).

## Analysis

- Consider the following strategy:
  - sellers of good quality  $\theta_G$  disclose their type
  - sellers of bad quality  $\theta_B$  do not disclose their type (and pool with uninformed)
- Equilibrium price is then given by

$$\begin{aligned} p(r_i = \theta_G) &= \theta_G \\ p(r_i = \emptyset) &= \frac{(1-\gamma)[\beta\theta_G + (1-\beta)\theta_B] + \gamma(1-\beta)\theta_B}{(1-\gamma) + \gamma(1-\beta)} > \theta_B \end{aligned}$$

- Why is this an equilibrium?

## Information Acquisition

- What if the seller (or the buyer) can make a costly investment to become informed prior to the sale? (Shavel, RAND 1994)
  - Mandatory vs. voluntary disclosure.
- Mandatory disclosure:
  - $p_G = \theta_G$  or  $p_B = \theta_B$  when informed (and is forced to disclose).
  - $p = \beta\theta_G + (1-\beta)\theta_B$  when uninformed.
  - No incentive to become informed since sellers get expected value anyway!
- Voluntary disclosure:
  - $p(r_i = \emptyset) = \frac{(1-\gamma)[\beta\theta_G + (1-\beta)\theta_B] + \gamma(1-\beta)\theta_B}{(1-\gamma) + \gamma(1-\beta)}$  when uninformed.
  - $p(r_i = \theta_G) = \theta_G$  or  $p(r_i = \emptyset)$  when informed.
  - Benefit from becoming informed:
$$\beta\theta_G + (1-\beta)p(r_i = \emptyset) - p(r_i = \emptyset) = \beta[\theta_G - p(r_i = \emptyset)] > 0$$
  - But incentives are socially inefficient because  $p(r_i = \emptyset) > \theta_B$ .

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