

Real options

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Key points

- Recognize the analogy between financial options and the investment decisions of financial managers
- Recognize the problems of NPV analysis when information is valuable.

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Structure of the lecture

- Review of NPV
- Real options
- An application

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Example

Type of Market	Probability of Market Type (Idiosyncratic)	Demand	Probability of Demand (Systematic)	Annual Cash flow
Berkeley, CA	0.8	High	0.25	\$32K
	0.8	Med	0.50	22
	0.8	Low	0.25	12
Cleveland, OH	0.2	High	0.25	22
	0.2	Med	0.50	12
	0.2	Low	0.25	2

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Example

- It costs 100K to make the initial investment
- Assume:
 - $r_f=2.1\%$
 - $\beta=1$
 - $E(r_m-r_f)=8.4\%$
 - $r_{\text{coffee}}=?$

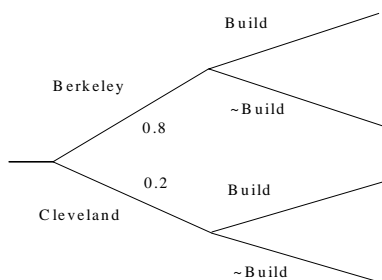
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Value of the project

- NPV Valuation:
- Can you do better?
- Hire a marketing research firm and value the project with the new information. What is the most you are willing to pay for the information?
- Early exercise

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To build or not to build



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Early exercise

- Remember that early exercise is not optimal for an American call option on a non dividend paying stock
- What if we have only ten years lease on the land for the coffee shop?
- Should we wait?

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Early exercise

- As our lease runs for 10 yrs, we give up one year of cashflows by waiting.
- Re-calculate the PV of the project

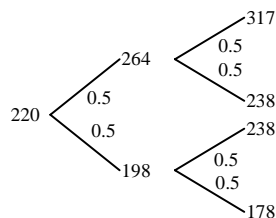
- The \$8.1K drop in value is like a dividend. We miss out on the dividend by not exercising early.

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Gold mine example

- We have the rights to operate a gold mine for three years. The mine produces 50K ounces. Costs of extraction: \$230/ounce. Gold is currently selling for \$220/ounces. The price of gold has a beta of 0. The risk free rate is 5%. First CF occurs immediately.

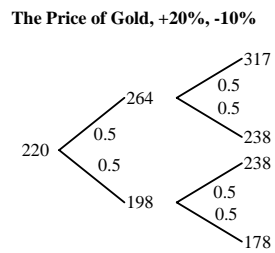
The Price of Gold, +20%, -10%



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Gold mine example

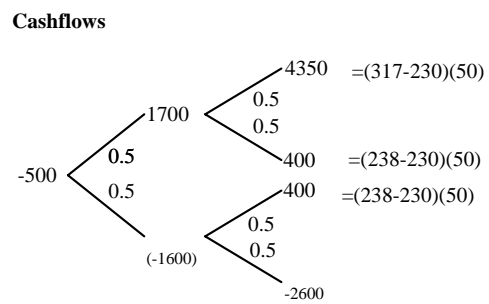
- Traditional NPV calculation:



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Opening and shutting down Options

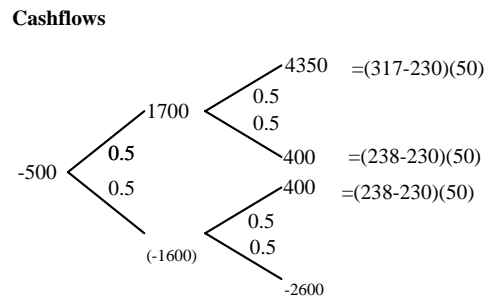
- What is wrong with our calculation?
- Open and close decisions.



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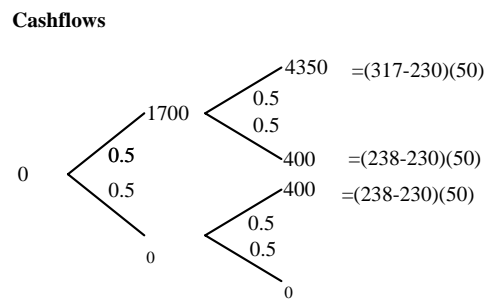
Opening and shutting down Options

- At the nodes with negative CF would you operate the mine?



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Opening and shutting down Options



- Replace zeros when the CF is negative and take NPV.
- NPV=

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Opening and shutting down options - Recognizing the option

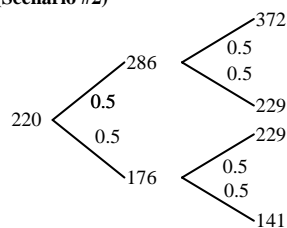
- What is the cash flow in each period when you take into account opening and shutting down options?

$$\text{Cashflow} = \text{Max} [50(\text{price of gold} - 230), 0]$$

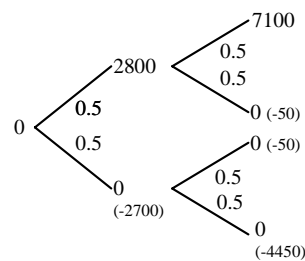
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Gold mine - Variance matters, +30%, -20%

**The Price of Gold
(Scenario #2)**



Cashflows for Scenario #2



$$\text{NPV}_{\text{GoldMine}} = 0 + .25 \left[\frac{2800}{(1+.05)} + \frac{7100}{(1+.05)^2} \right] + .25 \left[\frac{2800}{(1+.05)} \right] = 2943$$

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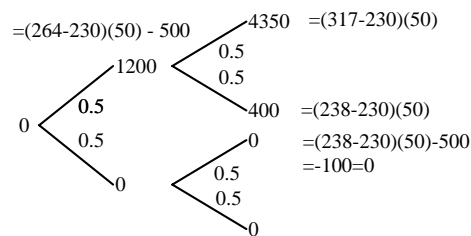
Costs to shutting down

- With opening and closing costs, the example become more realistic.
- It costs \$500K to open or shut down the mine.
- Now the cashflows depend not only on the price of gold, but also on whether the mine was open or closed last year

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Opening and shutting costs

Opening and Closing Costs



$$NPV_{GoldMine} = 0 + .5 \left[\frac{1200}{(1 + .05)} \right] + .25 \left[\frac{4350}{(1 + .05)^2} \right] + .25 \left[\frac{400}{(1 + .05)^2} \right] + 0 = 1649$$

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Opening and shutting costs

If the mine was open:

$$\begin{aligned}\text{Cashflow} &= \text{Max}[50(P_{\text{Gold}} - 230), -500]= \\ &= 50 * \text{Max}(P_{\text{Gold}} - 220, 0) - 500\end{aligned}$$

If the mine was closed:

$$\begin{aligned}\text{Cashflow} &= \text{Max}[50(P_{\text{Gold}} - 230) - 500, 0]= \\ &= 50 * \text{Max}[50(P_{\text{Gold}} - 240), 0]\end{aligned}$$

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Conclusion on opening and shutting costs

- Now the cashflows depend not only on the price of gold, but also on whether the mine was open or closed last year
- History matters. New entrant acts differently from an entrenched.

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Takeaway

- **Traditional NPV analysis may understate the value** of an investment when the investment project contains imbedded options.
- **Options are valuable when information is valuable.** Information is valuable when it affects real investment decisions.
- **Real options are a way to value flexibility.**

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