

Intangible capital, firm scope, and growth

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IT-related assets

[software, databases]

Intellectual property assets

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Organization capital

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This paper: Model emphasizing 2, with an application to long-run growth

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Property rights determine degree of exclusivity — e.g. patents vs. trade secrets

This paper

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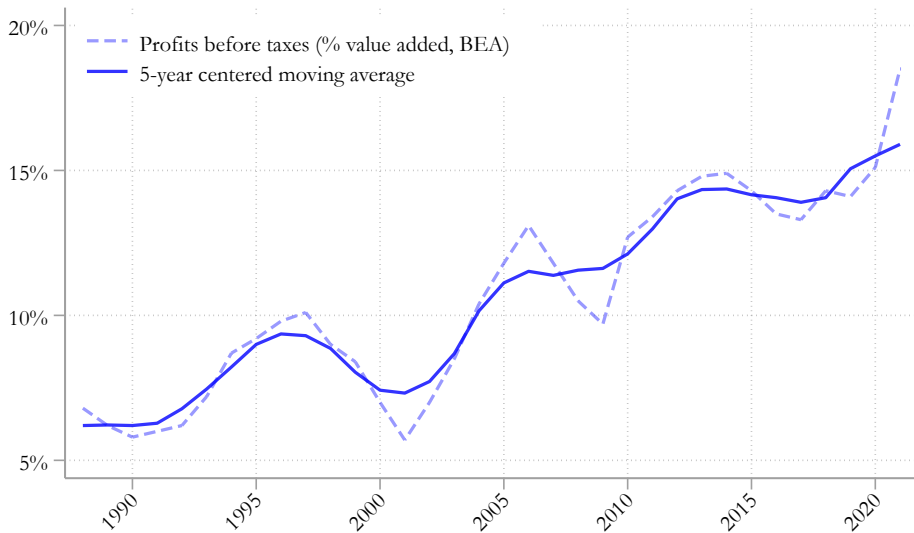
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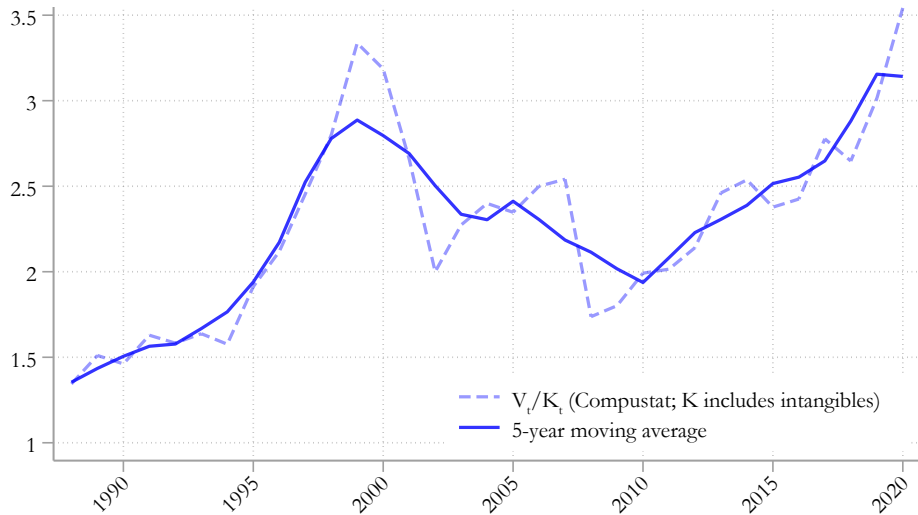
Transition: $\uparrow g$, entry, investment

Why is this (hopefully) interesting?

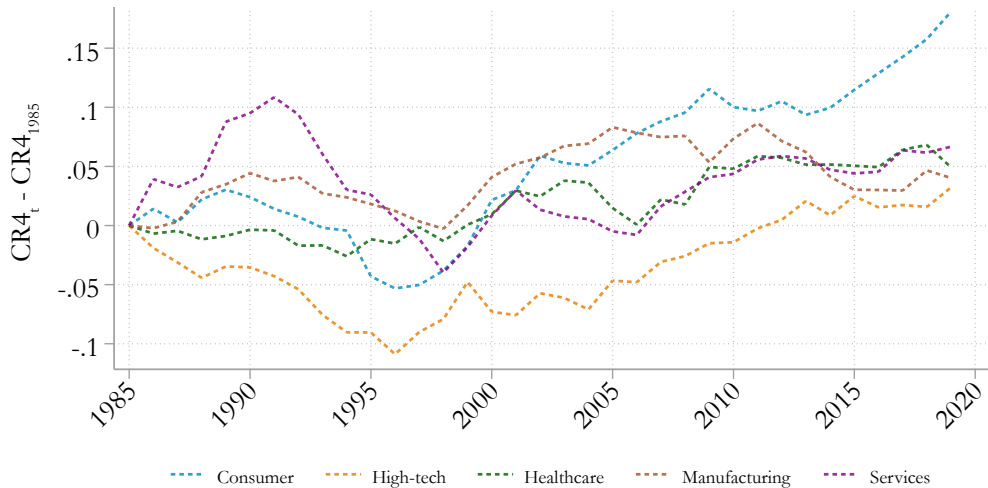
Corporate profits as a share of GDP have increased



Market valuations have increased

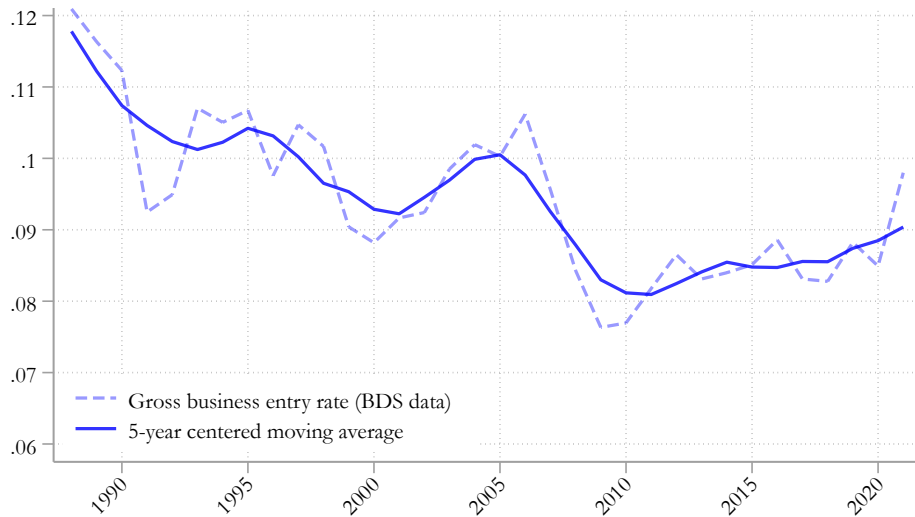


Concentration has increased



Compustat; NAICS-3D sectors weighted by sales.

Entry rates have fallen

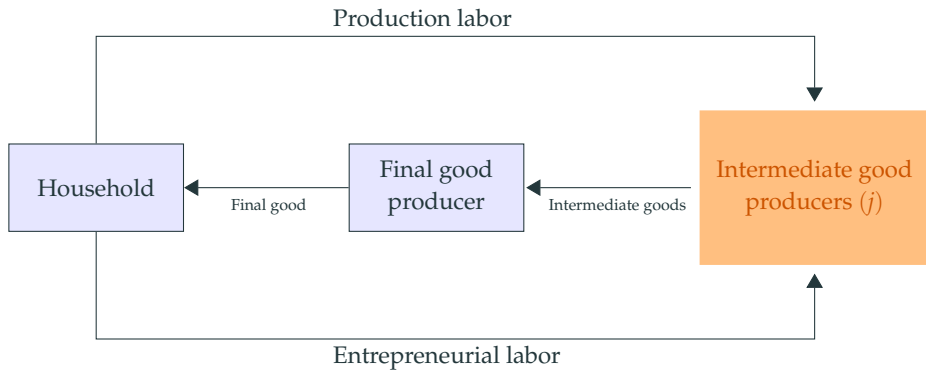


Roadmap

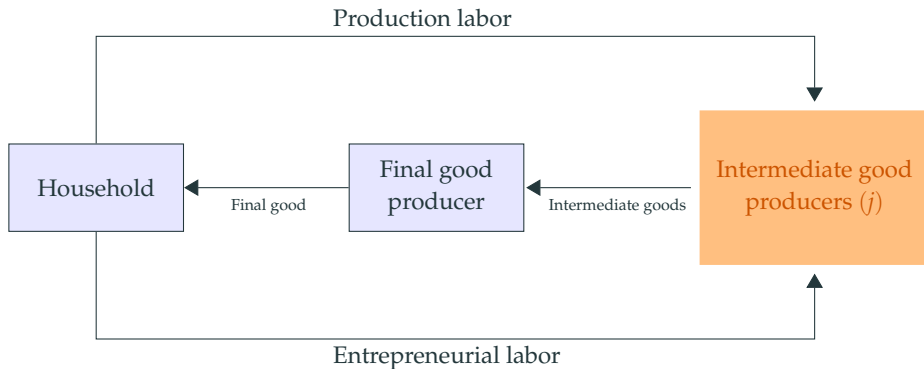
1. Model
2. Comparative statics
3. Data and transitional dynamics

1. Model

Structure

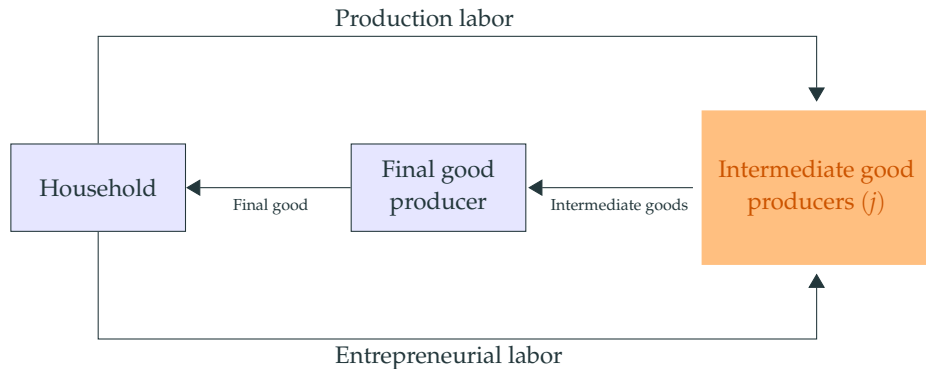


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$x_j \equiv$ **scope** of firm j

Household and final good producer

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Log utility

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e.g. machines, structures

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e.g. a patent for a touchscreen

using it for one product not reduce its availability for other products

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if $\rho > 0$, increasing returns to (x, n)

Non-exclusivity and the choice of scope

[Microfoundations]

What limits the scope of implementation?

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Assumption Entrepreneur only appropriates $1 - \gamma_t(x, \lambda)$ of enterprise value

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Non-exclusivity and the choice of scope

[Microfoundations]

Assumption Entrepreneur only appropriates $1 - \gamma_t(x, \lambda)$ of enterprise value

$$\overbrace{v_t^{(e)}(x, n)}^{\text{Entrepreneur surplus from entry}} = (1 - \gamma_t(x, \lambda)) \times \overbrace{v_t(x, n)}^{\text{Enterprise value}}, \quad \partial_x \gamma_t > 0, \quad \partial_{xx} \gamma_t \geq 0$$

$$\text{Optimal scope } x_t = \arg \max_x \overbrace{(1 - \gamma_t(x, \lambda))}^{(-) \text{ exclusivity}} \underbrace{x^{1-\omega+\rho\omega}}_{(+)\text{ non-rivalry}}$$

The creation of new intangibles

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1 unit of entrepreneurial labor

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1 unit of entrepreneurial labor \rightarrow intangible stock $n_t^{(e)}$

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created in $[t, t + dt]$

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=

$$\underbrace{L_{E,t}dt}$$

Total entrepreneurial
effort

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$$\begin{array}{c} \text{Total intangibles} \\ \text{created in } [t, t + dt] \\ \underbrace{dN_t^{(e)}} \end{array} = \underbrace{L_{E,t} dt}_{\text{Total entrepreneurial effort}} \times \underbrace{f(N_t^{(e)})}_{\text{Entrepreneurial productivity}}$$

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$$n_t^{(e)}$$

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[Romer, 1990]

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For now, spillovers from incumbents \rightarrow future entrants do not depend on ρ

Free-entry

$$L_{E,t} \geq 0 \quad \text{and} \quad v_t^{(e)} = W_t,$$

or

$$L_{E,t} = 0 \quad \text{and} \quad v_t^{(e)} \leq W_t.$$

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Equilibrium: $L_{E,t} + L_{Y,t} = 1$, $L_{Y,t}$ = Production labor demand from incumbents.

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Balanced growth path

For any $\rho \in [0, 1]$, if $\xi > 0$, there exists a unique equilibrium where $(x_t, L_{E,t})$ are constant and Y_t grows at rate $g > 0$.

2. Comparative statics

The effects of replicability

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$$\frac{dN_t^{(e)}}{N_t^{(e)}} = \xi L_E dt$$

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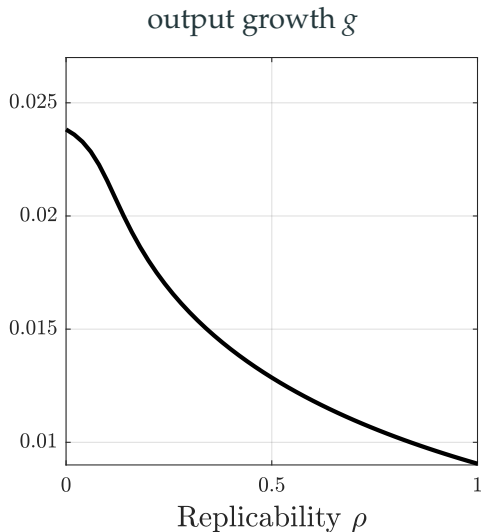
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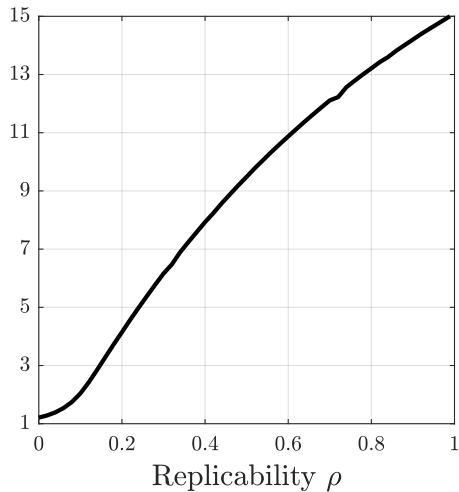
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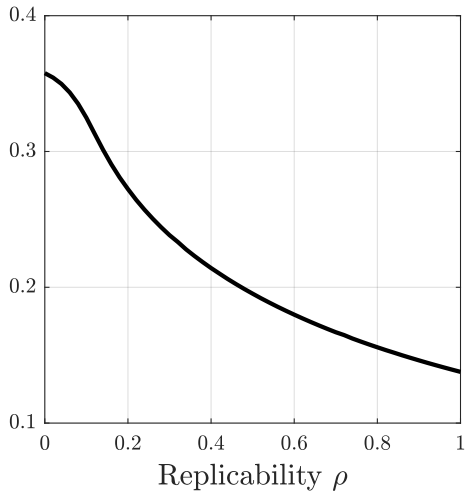


The effects of replicability

scope (x)



entry (L_E)



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[Adding spillovers]

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adding spillovers from incumbents \rightarrow future entrants may help offset this

Adding Spillovers

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Growth

$$g = (1 - \zeta) \xi L_E x^\beta$$

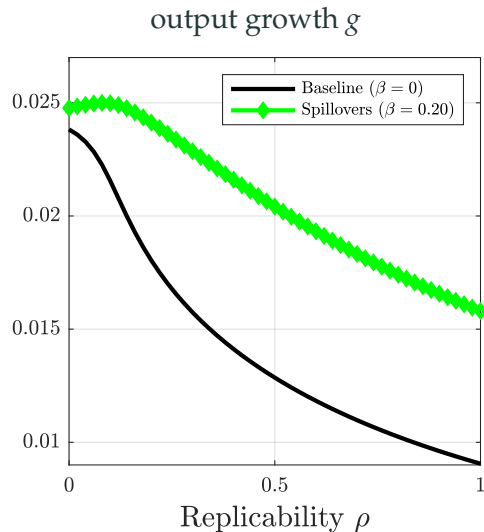
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Valuations and profits

Quantity, price, and user cost of capital

$$K_{N,t} = \int_0^{J_t} n_{j,t} dj \quad , \quad p_{K_{N,t}} = \frac{W_t}{n_t^{(e)}} \quad , \quad R_{N,t} dt = (r_t + \delta) dt - \frac{dp_{K_{N,t}}}{p_{K_{N,t}}}$$

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$$V_t = \underbrace{V_t^{(e)}}_{\text{entrepreneurs}} + \underbrace{\gamma V_t}_{\text{outsiders}}$$

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Aggregate Tobin's Q

$$Q_t = \frac{V_t}{p_{N,t} K_{N,t}} = \underbrace{\frac{1}{1 - \gamma}}_{\text{non-exclusivity}} \overbrace{\frac{R_N - \eta}{\omega(R_N - \eta) + (1 - \omega)\delta}}^{\text{market power}} > 1$$

Valuations and profits

Distribution of capital income

$$(1 - \zeta\chi)Y_t$$

(Capital income)

$$= R_N (p_{N,t}K_{N,t})$$

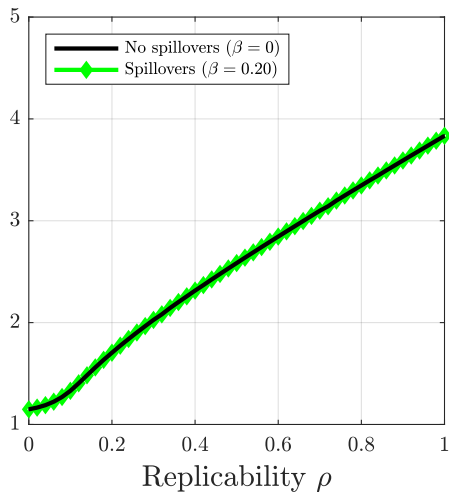
(Competitive capital cost)

$$+ (1 - \zeta\chi)Y_t \left(\underbrace{\gamma}_{\text{outsiders}} + \overbrace{(1 - \gamma)(1 - \omega) \frac{R_N - (\eta + \delta)}{R_N - \delta}}^{\text{entrepreneurs}} \right)$$

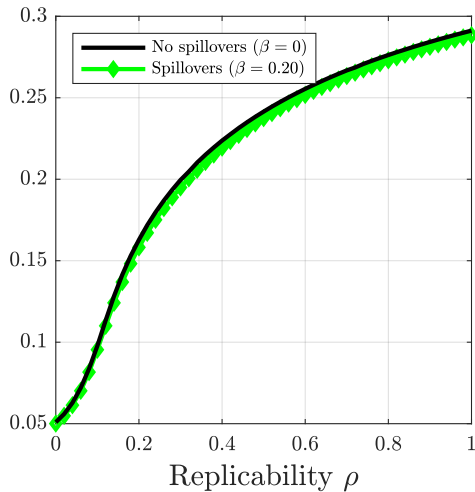
(Profits)

Valuations and profits

Tobin's Q



Profit share



Concentration and measured productivity

Concentration (HHI)

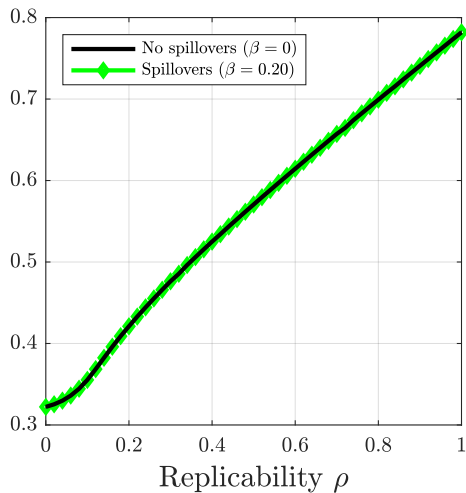
$$H_t = \int_{j=0}^{J_t} \left(x_{\tau(j)}^{1-(1-\rho_{\tau(j)})\omega} \left(\frac{n_{\tau(j)}}{N_t} \right)^\omega \right)^2 dj$$

Measured Productivity (Solow Residual)

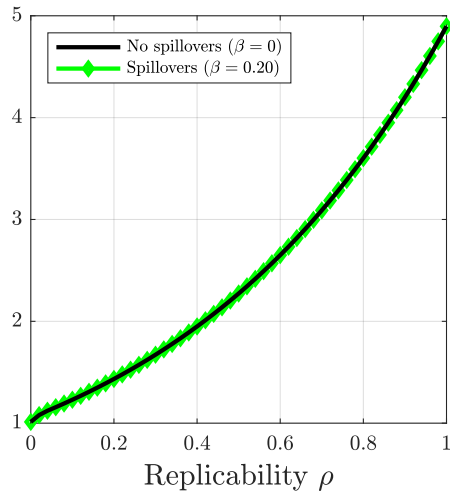
$$z = \underbrace{x^{(1-\zeta)\rho}}_{\text{Effect of replicability}} \underbrace{\left(x^{\frac{1-\omega}{\omega}} \frac{\xi x^\beta + \frac{\delta}{L_E}}{\left(\omega \xi x^\beta + \frac{\delta}{L_E} \right)^{\frac{1}{\omega}}} \right)^{1-\zeta}}_{\text{Effect of markups}}$$

Concentration and measured productivity

Concentration (HHI)



Solow Residual



Data and transitional dynamics

Calibrated parameters (1988-1992)

| Parameter | Description | Value | Source |
|-----------|-------------------------------|-------|---------------------------|
| η | Time discount rate | 0.02 | Annual calibration |
| ζ | Cobb-Douglas labor elasticity | 0.70 | Crouzet and Eberly (2023) |
| $1/\chi$ | Markup | 1.05 | Crouzet and Eberly (2023) |
| δ | Obsolescence rate | 0.11 | Gross exit rate (BDS) |
| β | Spillovers | 0 | TBD |
| ρ | Non-rivalry | | |

Data on firm scope

Hoberg and Phillips (2024)

US publicly traded firms, 1988-2021

How many product markets a firm operates in

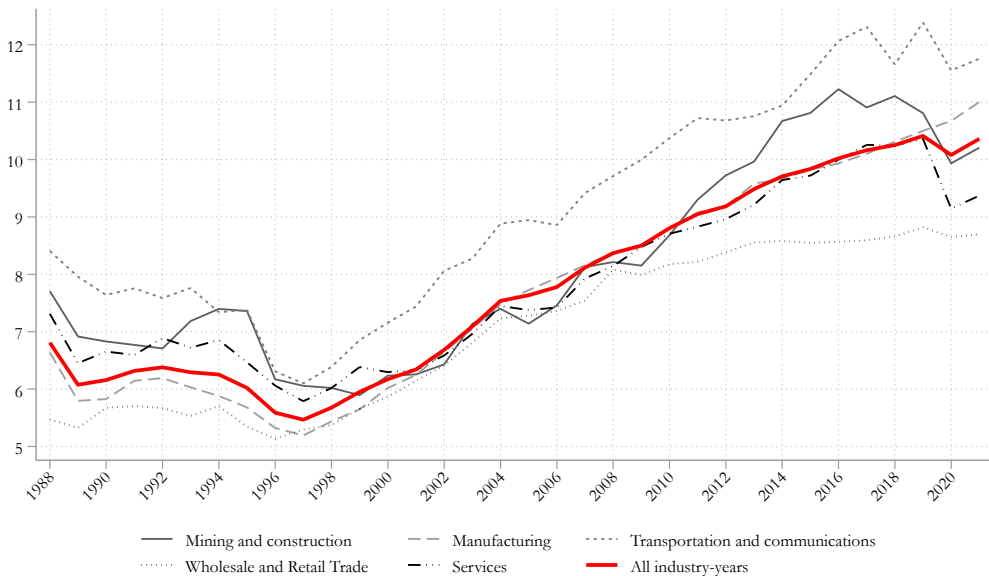
Obtained from textual analysis of 10K statements, Part I, item 1 (business description)

Advantages

Reporting required by Reg S-K

Available beyond consumer goods (Nielsen data)

Firm scope over time



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Empirical target for scope: $x = 6.3$ (average, 1988-1992)

The covariance between scope and sales

[Compustat sample and measure of n]

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[Compustat sample and measure of n]

Model

$$\text{Sales}_{j,t} \propto x_{j,t}^{1-\omega+\textcolor{brown}{p}\omega} n_{j,t}^{\omega}$$

The covariance between scope and sales

[Compustat sample and measure of n]

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$$\text{Sales}_{j,t} \propto x_{j,t}^{1-\omega+\rho\omega} n_{j,t}^{\omega}$$

Reduced-form

$$\log(\text{Sales}_{j,t}) = \alpha_{\text{ind}(j),t} + \rho_x \log(x_{j,t}) + \beta_n \log(n_{j,t}) + \epsilon_{j,t} \quad (1)$$

The covariance between scope and sales

[Compustat sample and measure of n]

| | 1988-1992 | 1988-2021 |
|-----------------|-------------------|-------------------|
| | (1) | (1) |
| $\log(x_{j,t})$ | 0.30*** (6.8) | 0.43*** (10.3) |
| $\log(n_{j,t})$ | 0.66*** (21.9) | 0.60*** (24.9) |
| obs. | 18700 | 140110 |
| s.e. clustering | $t \times ind$ | $t \times ind$ |
| industry f.e. | ✓ | ✓ |
| year f.e. | ✓ | ✓ |

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Model $Sales_{j,t} \propto x_{j,t}^{1-\omega+\rho\omega} n_{j,t}^{\omega}$

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Calibrated value $\rho = \frac{\beta_x - (1-\omega)}{\omega} = 0.18$

Data on ownership by founders and insiders

Firm sample: Firms with initial public offering (IPO), from Compustat/Execucomp

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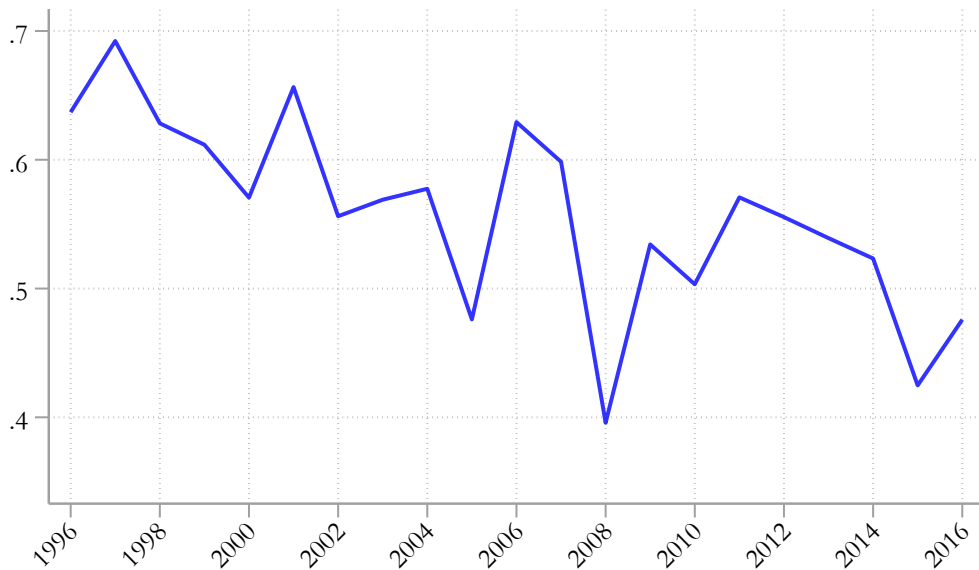
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Ownership shares



Matched moments (1988-1992)

[Other data sources] [Other calibrations]

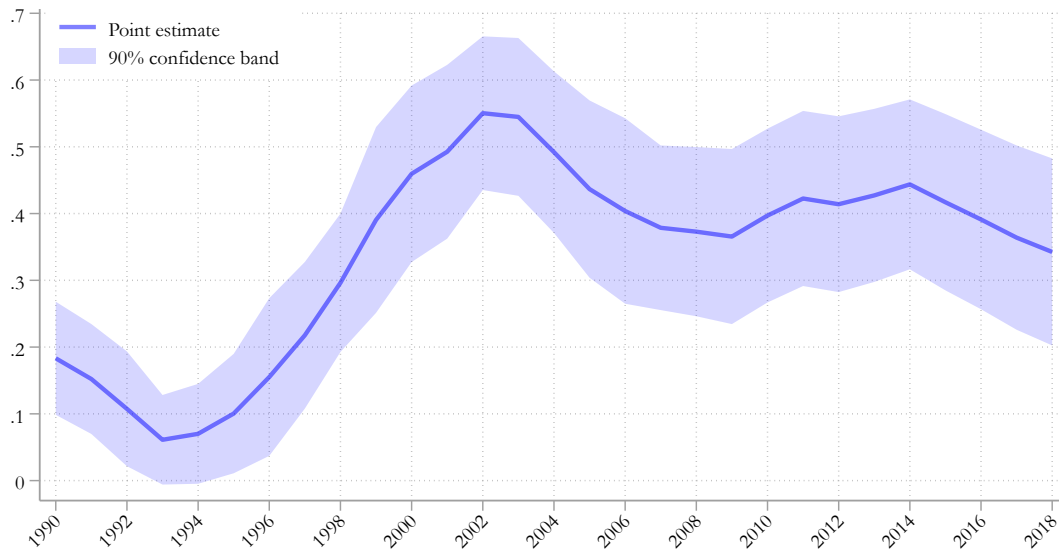
| Par. | Description | Par. value | Targeted moment | Model counterpart | Data value | Model value |
|-----------|----------------------|------------|-----------------|-------------------|------------|-------------|
| λ | Exclusivity | 1.54 | Outsider share | γ | 0.36 | 0.34 |
| α | Level of $\theta(x)$ | 2.64 | Average scope | x | 6.3 | 6.3 |
| κ | Slope of $\theta(x)$ | 1.32 | Tobin's Q | Q | 1.5 | 1.6 |
| ξ | Entr. productivity | 0.39 | Output growth | g | 0.027 | 0.027 |

In balanced growth,

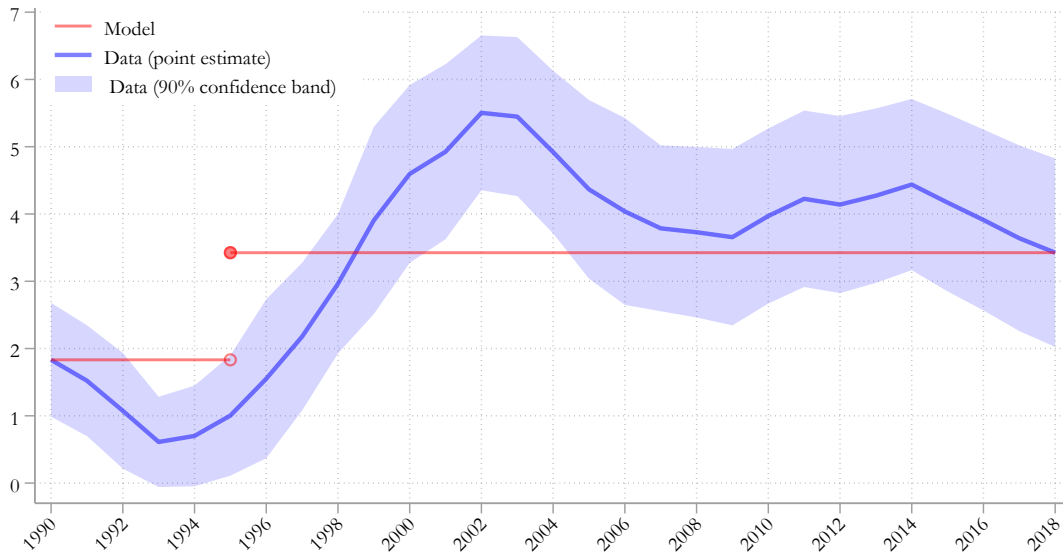
$$\gamma(x;\lambda) \propto \frac{\bar{x}}{x} \theta(x) \mu(\lambda)$$

$$\# \text{ outsiders needed to reach scope } x = \theta(x) = \max(0, \alpha(x - \bar{x})^\kappa)$$

Rolling window estimates of $\hat{\rho}$



The transition to a higher value of ρ



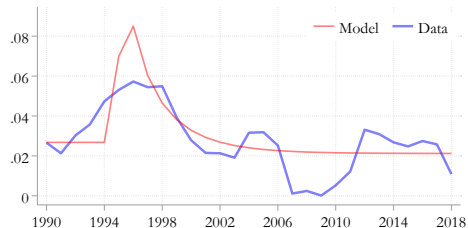
Balanced growth paths

[Other data sources] [Other calibrations]

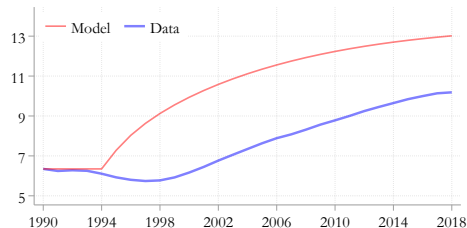
| | 1988-1992 | | 2016-2020 | |
|-----------------------|---------------|-------|---------------|-------|
| | $\rho = 0.18$ | | $\rho = 0.34$ | |
| Moment | Data | Model | Data | Model |
| Outsider share at IPO | 0.36 | 0.34 | 0.52 | 0.51 |
| Average scope | 6.3 | 6.3 | 10.1 | 13.6 |
| Tobin's Q | 1.5 | 1.6 | 2.8 | 2.1 |
| Output growth | 0.027 | 0.027 | 0.011 | 0.021 |

Aggregate dynamics

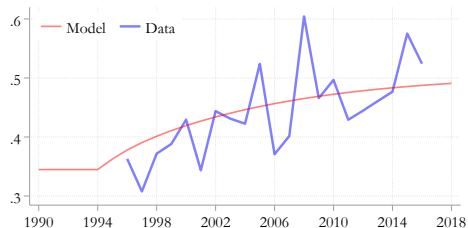
A: Output growth (g_t)



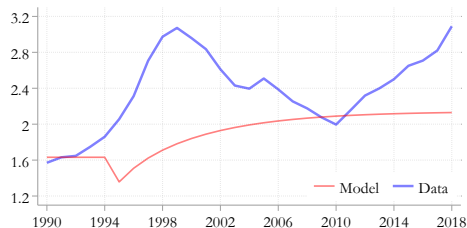
B: Average scope (\hat{x}_t)



C: Average outsider share (\hat{y}_t)

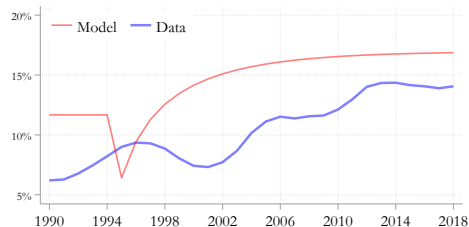


D: Aggregate Tobin's (Q_t)

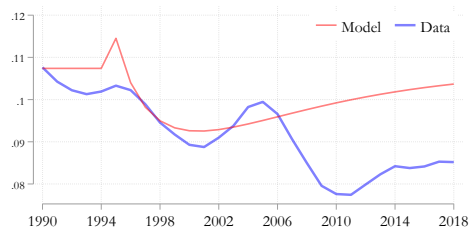


Aggregate dynamics

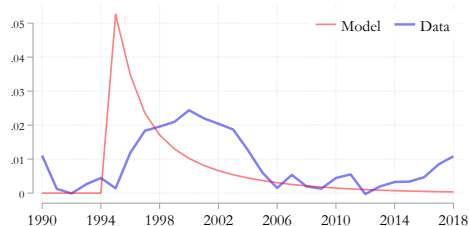
E: Aggregate profit share



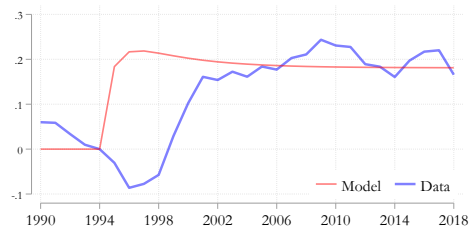
F: Gross entry rate



G: Measured TFP growth ($\hat{g}_{Z,t}$)



H: Concentration ($\log H_t$)



Conclusion

Conclusion

Q : Intangibles are partly non-rival in use. How does that affect growth?

A : $\uparrow \rho \not\Rightarrow \uparrow g$

Short run: $\uparrow g$

Long-run: $\downarrow g$ and \uparrow profits, valuations, concentration

Next :

Implications for the measurement of capital

Microfoundations

More

Non-exclusivity: microfoundations (1/3)

[Back]

For each m , entrepreneur "shares" / "stores" $n(m)$ with subset of employees ("outsiders")

$$\text{\# of outsiders per variety} = \frac{\theta(x)}{x}$$

$$\text{Total \# of outsiders} = \theta(x) \equiv \max(0, (x - \bar{x})^\kappa)$$

With intensity λ , each outsider receives right to start their own firm

Intangible capital $n(m)$; scope $\bar{x} < x$; Cournot competition

$\lambda \leftrightarrow$ **non-exclusivity**

$\lambda = 0$: full exclusivity

$\lambda = +\infty$: no exclusivity

$\lambda \in (0, +\infty)$: patents, trademarks, non-compete clauses

Non-exclusivity: microfoundations (2/3)

[Back]

Result At entry, the expected value of the right to compete to each outsider is:

$$v_t^{(c)} = \bar{x} \left(\frac{\psi v_t^{(e)}}{x_t} \right) \mu_t(\lambda), \quad \mu_t(\lambda) = \lambda \int_{s \geq t} e^{-\int_0^v (r_{t+u} + \lambda) du} \frac{A_{t+s} v_{t+s}}{A_t v_t} ds$$

where v_t is the price-earnings ratio of the firm under monopoly, and ψ is a constant.

Intuition

$$\overbrace{\pi_t^{(c)}(m)}^{\text{Manager profits per variety}} = \underbrace{s^{(c)} \times \overbrace{\pi_t(m)}^{\text{Firm profits in monopoly}}}_{\text{Cournot profits}} \times \underbrace{(1 - \varepsilon)}_{\text{Flow cost of competition}} \quad [\psi = (1 - \varepsilon)s^{(c)}] \quad (0.1)$$

$\mu_t(\lambda)$: "competitive pressure"

$[\mu_t(0) = 0$ — full exclusivity; $\mu_t(+\infty) = 1$ — no exclusivity]

Non-exclusivity: microfoundations (3/3)

[Back]

Entry deterrence To keep all employees from competing, entrepreneur must give them:

$$v_t^{(d)} = \int_0^{x_t} \frac{\theta(x_t)}{x_t} v_t^{(c)} dm = \theta(x_t) \bar{x} \left(\frac{\psi v_t^{(e)}}{x_t} \right) \mu_t(\lambda)$$

$$\implies \gamma_t(x_t; \lambda) = \theta(x_t) \bar{x} \left(\frac{\psi}{x_t} \right) \mu_t(\lambda)$$

If ψ is sufficiently low ($\epsilon \rightarrow 1, s^{(c)} \rightarrow 0$), deterrence is optimal to entrepreneur **ex-post**

\leftrightarrow collusion is possible for each variety

Cournot competition: details

Equation (0.1) can be derived from solving the Cournot game between the incumbent firm and a potential competitor. The solution pins down uniquely $s^{(c)}$, the ratio of Cournot profits of the potential entrant to the monopoly profits of the incumbent.

The main result is that $s^{(c)}$ only depends on (ζ, χ) , and the ratio ϕ of capital of the incumbent to the potential competitor.

The ratio of capital of the incumbent to the potential competitor is fixed. So, $s^{(c)}$ can be treated as a parameter.

Finally, let $s^{(inc,c)}$ denote the flow profits of the incumbent firm under Cournot competition, relative to their profits in monopoly. There can be cases where:

$$s^{(c)} + s^{(inc,c)} \geq 1,$$

i.e. Cournot competition generates more *total* profits than monopoly — even though it *always* generates less profits for the incumbent. In these cases deterrence might not be time-consistent for the incumbent.

In these cases, if the flow cost ε is large enough, it will remain profitable for the incumbent to deter entry.

Spillovers from incumbents to entrants

[Back]

Creation of new intangibles depends on scope of existing projects:

$$\frac{dN_t^{(e)}}{N_t^{(e)}} = \xi x_t^\beta L_{E,t} dt.$$

Interpretation:

New entrepreneurs receive ideas by observing existing firms.

Higher scope $x \rightarrow$ more new ideas generated.

Implications:

Depending on parameters, increasing ρ can lead to higher LR growth:

$\rho \uparrow \rightarrow x \uparrow \rightarrow$ higher growth.

Define

$$v_t = \int_{s \geq t} e^{-\int_0^v (r_{t+u} + \delta) du} \frac{A_{t+s}}{A_t} ds \quad [\text{Price-earnings ratio for entrants}]$$

$$\mu_t = \lambda \int_{s \geq t} e^{-\int_0^v (r_{t+u} + \lambda) du} \frac{A_{t+s} v_{t+s}}{A_t v_t} ds \quad [\text{Value of outsiders' option to compete}]$$

Then there exists sufficient states c_t such that:

$$v_t = v(c_t), \quad \mu_t = \mu(c_t), \quad L_{E,t} = L_E(c_t)$$

Given $L_E(\cdot)$, $v(\cdot)$, $\mu(\cdot)$ solve a system of coupled ODEs

The relative size of new entrants c_t is a sufficient state:

$$c_t = \left(\frac{n_t^{(e)}}{N_t} \right)^\omega, \quad N_t = \left(\int_j n_{j,t}^\omega dj \right)^{\frac{1}{\omega}}.$$

Equilibrium equations:

$$\left(\eta + x(\mu(c_t))^{1-(1-\rho)\omega} L_E(c_t) c_t\right) v(c_t) = 1 + \left(\omega \xi L_E(c_t) + \delta - x(\mu(c_t))^{1-(1-\rho)\omega} L_E(c_t) c_t\right) c_t f'(c_t)$$

$$\left(\lambda - \delta + \frac{1}{v(c_t)}\right) \mu(c_t) = \lambda + \left(\omega \xi L_E(c_t) + \delta - x(\mu(c_t))^{1-(1-\rho)\omega} L_E(c_t) c_t\right) c_t \mu'(c_t)$$

$$0 = \min \left(L_E(c_t), 1 - \frac{1 - \zeta \chi}{\zeta \chi} x(\mu(c_t))^{1-(1-\rho)\omega} (1 - \gamma(x(\mu(c_t)), \mu(c_t))) (1 - L_E(c_t)) c_t v(c_t) \right)$$

The functions $x(\mu)$ and $\gamma(x; \mu)$ are state-invariant and given by:

$$\gamma(x; \mu) = s_\pi \frac{\theta(x)}{x} \bar{x} \mu$$

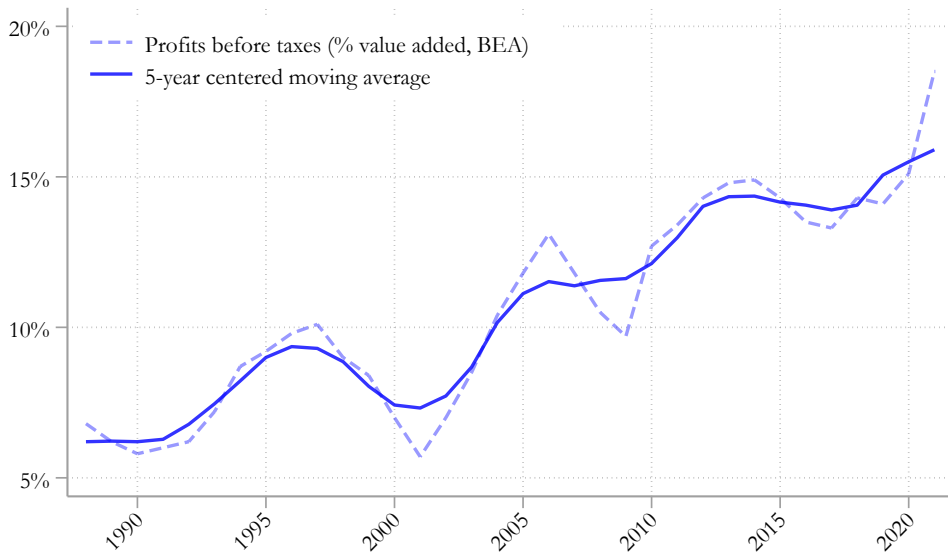
$$x(\mu) = \arg \max_x (1 - \gamma(x; \mu)) x^{1-(1-\rho)\omega}$$

with s_π from the Cournot game.

This system can be solved using finite-difference methods.

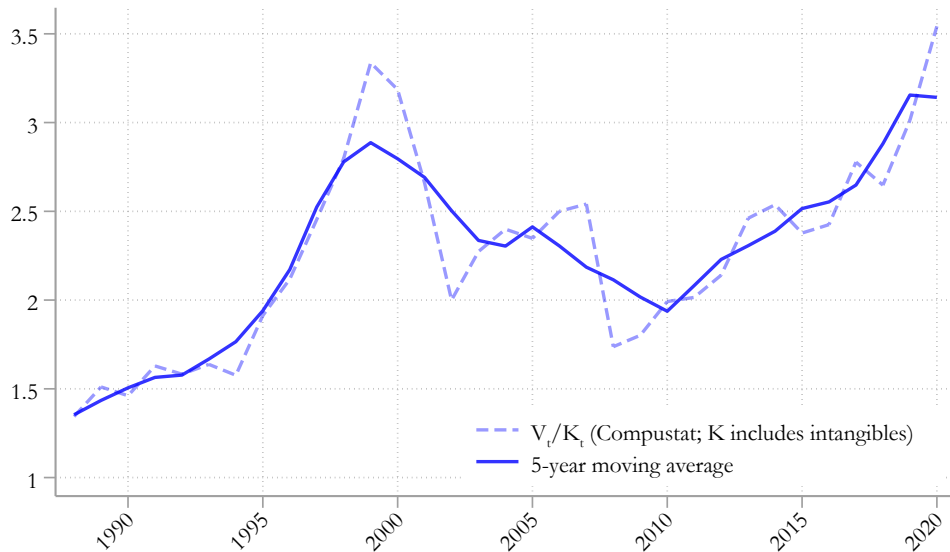
Other data sources: Profit rates (BEA)

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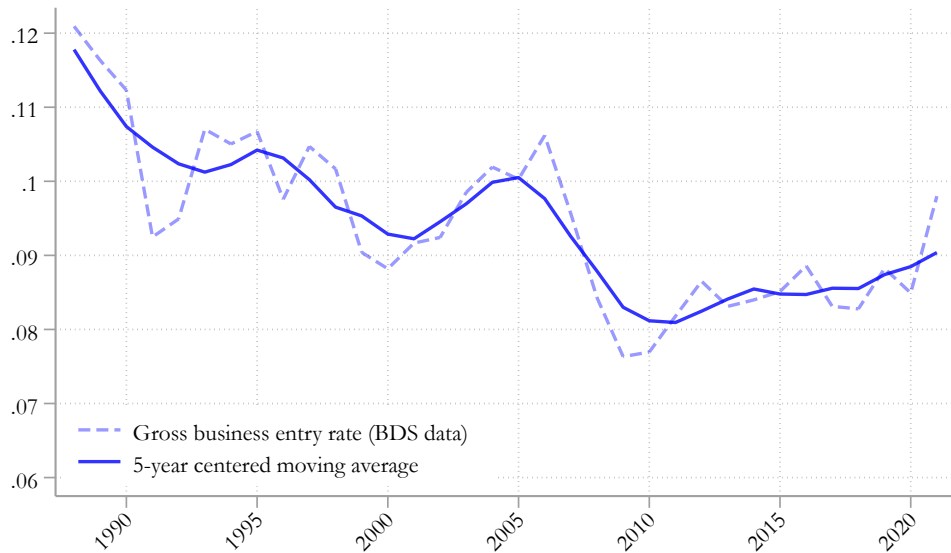
Other data sources: Tobin's Q (Compustat)

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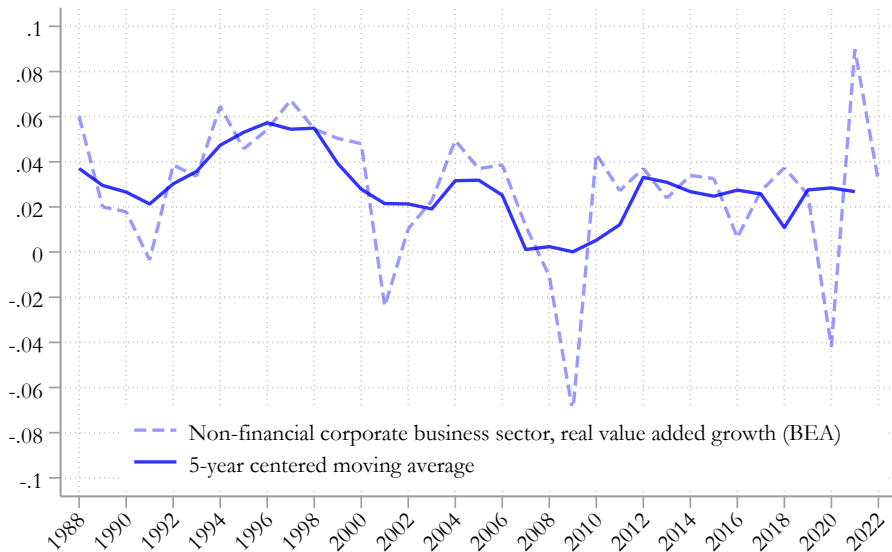
Other data sources: Gross entry rates (BDS)

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Other data sources: Growth rates (BEA)

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Consider the model with no delay ($\lambda = +\infty$), but calibrate ε , subject to: $\varepsilon \geq \underline{\varepsilon}(\zeta, \phi)$.

| Par. | Description | Par. value | Targeted moment | Model counterpart | Data value | Model value |
|---------------|----------------------|------------|-----------------------|-------------------|------------|-------------|
| ε | Entry cost | 0.89 | Outsider share at IPO | γ | 0.35 | 0.34 |
| α | Level of $\theta(x)$ | 2.37 | Average scope | x | 6.3 | 6.3 |
| κ | Slope of $\theta(x)$ | 1.34 | Tobin's Q | Q | 1.5 | 1.6 |
| ξ | Entr. productivity | 0.38 | Output growth | g | 0.027 | 0.027 |

In balanced growth,

$\gamma(x; \lambda) \propto \frac{\bar{x}}{x} \theta(x) \mu(\lambda)$

outsiders needed to reach scope x = $\theta(x)$ = $\max(0, \alpha(x - \bar{x})^\kappa)$

Consider the model with delay ($\lambda < +\infty$), but set $\varepsilon = 0$.

| Par. | Description | Par. value | Targeted moment | Model counterpart | Data value | Model value |
|-----------|----------------------|---------------|-----------------------|----------------------|---------------|----------------|
| λ | Exclusivity | 1.35 | Outsider share at IPO | γ | 0.35 | 0.34 |
| α | Level of $\theta(x)$ | 0.27 | Average scope | x | 6.3 | 6.3 |
| κ | Slope of $\theta(x)$ | 1.34 | Tobin's Q | Q | 1.5 | 1.6 |
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Consider the model with no delay ($\lambda = +\infty$), but calibrate ε , subject to: $\varepsilon \geq \underline{\varepsilon}(\zeta, \phi)$.

| | 1988-1992 | | 2016-2020 | |
|-----------------------|---------------|-------|---------------|-------|
| | $\rho = 0.18$ | | $\rho = 0.34$ | |
| Moment | Data | Model | Data | Model |
| Outsider share at IPO | 0.35 | 0.32 | 0.50 | 0.53 |
| Average scope | 6.3 | 6.3 | 10.1 | 16.0 |
| Tobin's Q | 1.5 | 1.6 | 2.8 | 2.3 |
| Output growth | 0.027 | 0.027 | 0.011 | 0.021 |

Consider the model with no delay ($\lambda = +\infty$), but set $\varepsilon = 0$.

| | 1988-1992 | | 2016-2020 | |
|-----------------------|---------------|-------|---------------|-------|
| | $\rho = 0.18$ | | $\rho = 0.34$ | |
| Moment | Data | Model | Data | Model |
| Outsider share at IPO | 0.35 | 0.32 | 0.50 | 0.53 |
| Average scope | 6.3 | 6.3 | 10.1 | 15.4 |
| Tobin's Q | 1.5 | 1.6 | 2.8 | 2.3 |
| Output growth | 0.027 | 0.027 | 0.011 | 0.021 |