

Discussion of  
“Asset Pricing Implications of Systemic Risk in Network Economies”  
Buraschi and Tebaldi (2019)

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# Economic and Financial Networks

- Growing literature on how network linkages between firms, banks, industries can
  - (i) function as a mechanism for propagation and amplification of shocks.
  - (ii) translate micro shocks into aggregate fluctuations.
  
- Applications:
  - ▶ potential explanation for the source of macroeconomic fluctuations
  - ▶ a theory of systemic risk in the banking system
  
- [This paper](#): asset pricing implications of network interactions

# This Paper

- **Framework:** endowment economy of  $n$  firms with interlinked dividend streams
  - ▶ network  $\Delta$  capturing the likelihood of distress spillovers (reduction in dividends)
  - ▶ study whether the distress can persist for a long time due to spillovers
  - ▶ **subcritical regime:** idiosyncratic shocks die out very rapidly
  - ▶ **supercritical regime:** the distress can persist in the long run in a large economy
  
- **Main Takeaways:**
  - ▶ the threshold between the two phases depends on the network  $\Delta$
  - ▶ higher  $\Delta_{ij}$  results in more spillovers and faster transition to the supercritical regime
  - ▶ all this has to be priced ex ante: a model of **endogenous long-run risk**

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# Model

- Economy consisting of  $n$  firms with dividend streams

$$d_{it} = (a_i - \epsilon_i H_{it}) Y_t$$

- ▶  $Y_t$ : common systematic shock (following  $dY_t/Y_t = \mu dt + \sigma dW_t$ )
  - ▶  $a_i$ : payout in the normal state
  - ▶  $\epsilon_i$ : reduction in the distress state
  - ▶  $H_{it} \in \{0, 1\}$ : binary variable indicating the distress state
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- $H_{it}$  transitions between 0 and 1 following independent jump processes:
    - ▶  $\lambda_i$ : transition rate to distress ( $0 \rightarrow 1$ )
    - ▶  $\eta_i$ : transition rate out of distress ( $1 \rightarrow 0$ )

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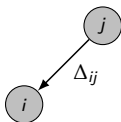
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## Model: Network Interdependence

- While transitions occur independently, transition rates are intertwined.  
Distress at some firm  $j$  increases the likelihood of distress at other firms:

$$\lambda_i(\mathbf{H}) = \lambda_i + \lambda \sum_{j=1}^n \Delta_{ij} H_j$$

- Network of distress spillovers:  $\Delta$



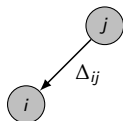
- Recovery rates not subject to spillovers:  $\eta_i(\mathbf{H}) = \eta$ 
  - ▶ extreme asymmetry in how negative and positive shocks propagate!

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# Markovian Model

- A Markovian model of transitions in and out of distress:

$$d_{it} = (a_i - \epsilon_i H_{it}) Y_t$$

$$\lambda_i = \lambda \sum_{j=1}^n \Delta_{ij} H_j$$

$$\eta_i = \eta.$$

- **Key question:** suppose we start from a no distress state ( $\mathbf{H} = 0$ ) and push one firm to distress ( $H_i = 0 \rightarrow H_i = 1$ ). How long does it take for the system to get back to the full no distress state?
- **Solution:** use standard results for Markov chain convergence times to quantify this time as a function of  $\Delta$ .

# Cascades

## Definition

A sequence of economies experiences a **cascade** if expected time to mixing of the Markov chain grows exponentially in  $n$ .

$$\lim_{n \rightarrow \infty} \frac{1}{n} \log \mathbb{E}[T_{\text{mix}}] > 0.$$

- Cascade: distress can persist for a very long time.

## Theorem

*There exists a critical threshold  $\kappa(\Delta)$  such that a cascade can occur with positive probability if and only if  $\lambda/\eta > \kappa(\Delta)$ .*

- Two very different regimes:
  - ▶ **subcritical**: the effect of shocks die out in a large economy in the long run
  - ▶ **supercritical**: the effect of shocks last for a long time even in a large economy

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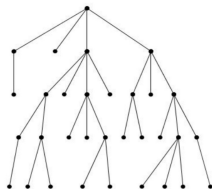
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## Intuition

- A network where each agent has  $m$  neighbors:

$$\begin{cases} \text{subcritical:} & m\lambda < \eta \\ \text{supercritical:} & m\lambda > \eta \end{cases}$$



- If  $m$  is large relative to the recovery rate, one distressed firm can infect many many others. But if  $m$  is small, the infection dies out.

## Asset Pricing Implications

- If initial shocks do not dissipate away in the long run, then they should be priced.
- A model of generating long-run risks endogenously.
- Long term risk premium:

$$\mu_{\infty}^i = \gamma\sigma^2 + (h_{i\infty}\epsilon/a) * (\text{network-dependent terms})$$

- In the **supercritical regime** ( $h_{i\infty} > 0$ ), we no longer have a single-factor model.
- Therefore, CAPM  $\beta$  no longer captures priced risk exposure.

## Comment

- Modeling assumptions indispensable to the creating long-lasting effects:
  - (i) asymmetric propagation between positive and negative shocks
  - (ii) epidemic-like propagation mechanism (“neighborhood independence”)
  
- No reason to think the assumptions are unreasonable in principle
- Question: what environment the model is approximating?
  - ▶ in general, macro predictions of network models are highly sensitive to the assumptions made on micro interactions ([Acemoglu et al., 2016](#))

## Comment

$$\lambda_i(\mathbf{H}) = \lambda \sum_{j=1}^n \Delta_{ij} H_j$$

- The model has two key features:
  - (1) **out-neighborhood independence:**  
likelihood that  $j$  infects  $i$  is independent of how many others  $j$  can infect
  - (2) **in-neighborhood independence:**  
likelihood that  $j$  infects  $i$  is independent of how many others can infect  $i$ .
- Both forces imply more connections can only intensify the likelihood of cascades.
- Reasonable assumptions for epidemics and pandemics
  - ▶ You cannot diversify the risk of getting sick by hanging out with more people!



## Comment

- More questionable for spillovers via economic interactions or financial markets:  
**holding the exposure of  $i$  to  $j$  constant**, changing  $i$  or  $j$ 's other connections can still change the propagation intensity.
  - ▶ **production networks:**  
unless inputs are perfect complements, having more suppliers reduces the likelihood of spillover from a given supplier (in-neighborhood dependence)
  - ▶ **interbank networks:**  
the likelihood of spillover of losses from debtor  $j$  to creditor  $i$  depends not only on  $i$ 's exposure to  $j$ , but also on how much  $j$  owes others (out-neighborhood dependence)
- How important is this very strong propagation mechanism for the existence of a supercritical regime?

# Summary

- Nice and innovative paper aimed at studying the asset pricing implications of network economies
- Analytical results on how firm-level shocks can persist for a very long time
  - ▶ phase transition and sub- vs. supercritical regimes
  - ▶ risk premia
  - ▶ characterization in terms of network centralities (see the paper)
- **Comments/Wishlist:** like any other model, results are sensitive to the specific propagation mechanism assumed in the model
  - ▶ holding interaction levels constant, shocks to neighbors cannot be diversified away
  - ▶ key in generating long-lasting effects
  - ▶ important to argue for contexts/applications where such assumptions are good approximations